

## Math

Grade 10- H.O.T problems Chapter 1 {Lessons 1,2,3,4,5 and 6}

Name: .....

Grade:10

Duration: (1 hour - 60 min )

Section: .....

### Lesson 1-1 Expressions and Formulas H.O.T problems

**Q1:- FIND THE ERROR** Lauren and Rico are evaluating  $\frac{-3d - 4c}{2ab}$  for  $a = -2$ ,  $b = -3$ ,  $c = 5$ , and  $d = 4$ . Is either of them correct? Explain your reasoning.

Lauren

$$\begin{aligned}\frac{-3d - 4c}{2ab} &= \frac{-3(4) - 4(5)}{2(-2)(-3)} \\ &= \frac{-12 - 20}{12} = \frac{-32}{12} = -\frac{8}{3}\end{aligned}$$

Rico

$$\begin{aligned}\frac{-3d - 4c}{2ab} &= \frac{-3(4) - 4(5)}{2(-2)(-3)} \\ &= \frac{-12 - 20}{12} = \frac{8}{12} = \frac{2}{3}\end{aligned}$$

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**Q2:- CHALLENGE** Let  $m$ ,  $n$ ,  $p$ , and  $q$  represent nonzero positive integers. Find a number in terms of  $m$ ,  $n$ ,  $p$ , and  $q$  that is halfway between  $\frac{m}{n}$  and  $\frac{p}{q}$ .

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**The end of Sec. 1.1**

**Lesson 1-2 Properties of Real Numbers**  
**H.O.T problems**

**Q1:-WHICH ONE DOESN'T BELONG?** Identify the number that does not belong with the other three. Explain your reasoning.

$$\sqrt{21}$$

$$\sqrt{35}$$

$$\sqrt{67}$$

$$\sqrt{81}$$

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**Q2:- FIND THE ERROR** Luna and Sophia are simplifying  $4(14a - 10b) - 6(b + 4a)$ . Is either of them correct? Explain your reasoning.

*Luna*

$$\begin{aligned} 4(14a - 10b) - 6(b + 4a) \\ 56a - 40b - 6b + 24a \\ 80a - 46b \end{aligned}$$

*Sophia*

$$\begin{aligned} 4(14a - 10b) - 6(b + 4a) \\ 56a - 40b - 6a - 24b \\ 50a - 64b \end{aligned}$$

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**Q3:- REASONING** Determine whether the following statement is *sometimes*, *always*, or *never* true. Explain your reasoning.

*An irrational number is a real number within a radical sign.*

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**The end of Sec. 1.2**

**Lesson 1-3 Solving Equations**  
**H.O.T problems**

**Q1:- FIND THE ERROR** Steven and Jade are solving  $A = \frac{1}{2}h(b_1 + b_2)$  for  $b_2$ . Is either of them correct? Explain your reasoning.

Steven

$$A = \frac{1}{2}h(b_1 + b_2)$$
$$\frac{2A}{h} = (b_1 + b_2)$$
$$\frac{2A - b_1}{h} = b_2$$

Jade

$$A = \frac{1}{2}h(b_1 + b_2)$$
$$\frac{2A}{h} = (b_1 + b_2)$$
$$\frac{2A}{h} - b_1 = b_2$$

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**The end of Sec. 1.3**

**Lesson 1-4 Solving Absolute Value Equations**  
**H.O.T problems**

**Q1:-FIND THE ERROR** Ana and Ling are solving  $|3x + 14| = -6x$ . Is either of them correct? Explain your reasoning.

| Ana                                        | Ling                                       |
|--------------------------------------------|--------------------------------------------|
| $ 3x + 14  = -6x$                          | $ 3x + 14  = -6x$                          |
| $3x + 14 = -6x$ or $3x + 14 = 6x$          | $3x + 14 = -6x$ or $3x + 14 = 6x$          |
| $9x = -14$ $14 = 3x$                       | $9x = -14$ $14 = 3x$                       |
| $x = -\frac{14}{9}$ ✓ $x = \frac{14}{3}$ ✓ | $x = -\frac{14}{9}$ ✗ $x = \frac{14}{3}$ ✓ |

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**The end of Sec. 1.4**

## Lesson 1-5 Solving Inequalities

### H.O.T problems

**Q1:- FIND THE ERROR** Madlynn and Emilie were comparing their homework. Is either of them correct? Explain your reasoning.

*Madlynn*

$$\frac{4x+5}{-2} - 1 > -3$$
$$\frac{4x+5}{-2} < -2$$
$$4x+5 > 4$$
$$4x > -1$$
$$x > -\frac{1}{4}$$

*Emilie*

$$\frac{4x+5}{-2} - 1 > -3$$
$$\frac{4x+5}{-2} > -2$$
$$4x+5 > 4$$
$$4x > -1$$
$$x > -\frac{1}{4}$$

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**Q2:- WRITING IN MATH** Why does the inequality symbol need to be reversed when multiplying or dividing by a negative number?

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**The end of Sec. 1.5**

## Lesson 1-6 Solving Compound and Absolute Value Inequalities

### H.O.T problems

**Q1:- FIND THE ERROR** David and Sarah are solving  $4|-5x - 3| - 6 \geq 34$ . Is either of them correct? Explain your reasoning.

| David                                       | Sarah                                       |
|---------------------------------------------|---------------------------------------------|
| $4 -5x - 3  - 6 \geq 34$                    | $4 -5x - 3  - 6 \geq 34$                    |
| $ -5x - 3  \geq 10$                         | $ -5x - 3  \geq 10$                         |
| $-5x - 3 \geq 10$ or $-5x - 3 \leq -10$     | $-5x - 3 \leq 10$ or $-5x - 3 \geq -10$     |
| $-5x \geq 13$ $-5x \leq -7$                 | $-5x \leq 13$ $-5x \geq -7$                 |
| $x \leq -\frac{13}{5}$ $x \geq \frac{7}{5}$ | $x \geq -\frac{13}{5}$ $x \leq \frac{7}{5}$ |

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**Q2:- REASONING** Determine whether each statement is *true* or *false*. If false, provide a counterexample.

The graph of a compound inequality involving an *and* statement is bounded on the left and right by two values of  $x$ .

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**Q3:- WHICH ONE DOESN'T BELONG?** Identify the compound inequality that is not the same as the other three. Explain your reasoning.

|              |                     |                     |                       |
|--------------|---------------------|---------------------|-----------------------|
| $-3 < x < 5$ | $x > 2$ and $x < 3$ | $x > 5$ and $x < 1$ | $x > -4$ and $x > -2$ |
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**Q4:- WRITING IN MATH** Summarize the difference between *and* compound inequalities and *or* compound inequalities.

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The end of Sec. 1.6